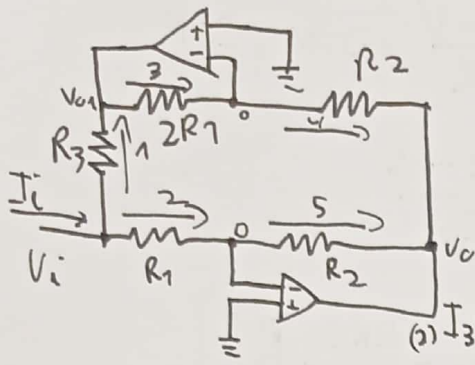


1 | Impedancia de entrada. Condición ∞ . Diseño para $A_V = -10 V/V$



$$(1) I_i = I_2 + I_1$$

$$I_i = \frac{V_i - 0}{R_1} + \frac{V_i - V_{01}}{R_3}$$

$$(2) I_3 = I_4 \quad \frac{V_{01} - 0}{2R_1} = \frac{0 - V_0}{R_2} \rightarrow V_{01} = -\frac{2R_1}{R_2} V_0 = +\frac{2R_1 R_2}{R_2 R_1} V_1 = 2V_i$$

$$(3) I_2 = I_5 \quad \frac{V_i - 0}{R_1} = \frac{0 - V_0}{R_2} \rightarrow V_i = -\frac{R_1}{R_2} V_0 \rightarrow V_0 = -\frac{R_2}{R_1} V_i$$

- Sustituimos 2 en 1

$$I_i = \cancel{\frac{V_i}{R_1}} + \cancel{\frac{V_i}{R_3}} - \cancel{\frac{V_i}{R_3}} = \frac{V_i}{R_1}$$

$$I_i = V_i \left(\frac{1}{R_1} + \frac{1}{R_3} \right) - \frac{2V_i}{R_3} = V_i \left(\frac{R_3 - R_1}{R_3 R_1} \right) \rightarrow R_i = \frac{V_i}{I_i} = \frac{R_3 R_1}{R_3 - R_1}$$

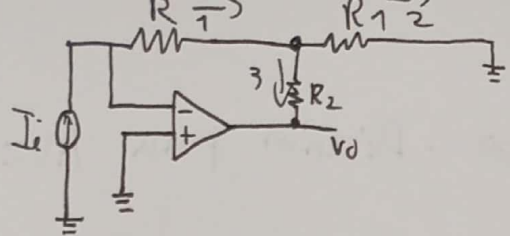
- La condición para $R_i \rightarrow \infty$ $R_3 - R_1 = 0 \rightarrow \boxed{R_3 = R_1}$

- La ecuación $V_0 = A_V V_{in}$ la obtuvimos en (3)

$$V_0 = -\frac{R_2}{R_1} V_i \rightarrow A_V = +\frac{R_2}{R_1} = +10 \rightarrow R_2 = 10 R_1$$

Pongamos $R_1 = 1 \text{ k}\Omega$ por lo que $R_2 = 10 \text{ k}\Omega$

2



a) exp. tens. salida y transimpedancia

$$I_i = I_2 + I_3 \quad I_i = I_1 = \frac{0 - V}{R} \rightarrow V = -I_i R$$

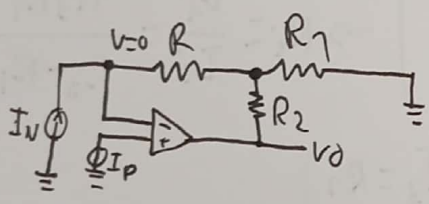
$$I_i = \frac{V - 0}{R_1} + \frac{V - V_0}{R_2} = -\frac{I_i R}{R_1} + \frac{-I_i R - V_0}{R_2}$$

$$I_i \left(1 + \frac{R}{R_1} + \frac{R}{R_2} \right) = -\frac{V_0}{R_2} \rightarrow \left[V_0 = -I_i \left(R_2 + \frac{R R_2}{R_1} + R \right) \right]$$

$$\left[R_m = \frac{V_0}{I_i} = - \left(R_2 + \frac{R R_2}{R_1} + R \right) \right]$$

b) Corrientes de pol.

Quitamos I_i a unid. abierto y añadimos I_N e I_P

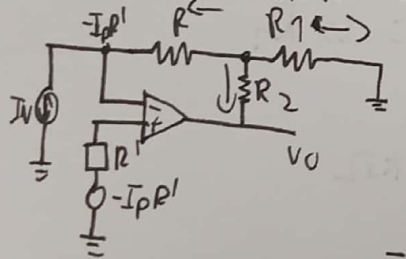


Como por + no puede entrar corriente I_P es como si estuviera entre 2 tierras por lo que no afecta.

I_N no afecta por estar tambien entre 2 tierras

¿? Tengo dudas de esto, yo creo que habra que hacer el analisis con I_N

c) Para solucionarlo añadimos una resistencia a I_P



$$V(+)=V(-) = -I_P R'$$

$$I_N = \frac{+I_P R' + V}{R} \rightarrow V = \pm (I_P R' + I_N R)$$

$$-I_N = \cancel{\frac{V-0}{R_1}} + \cancel{\frac{V-V_0}{R_2}} \rightarrow \frac{V_0}{R_2} = \pm I_N - \frac{V}{R_1} \mp \frac{V}{R_2}$$

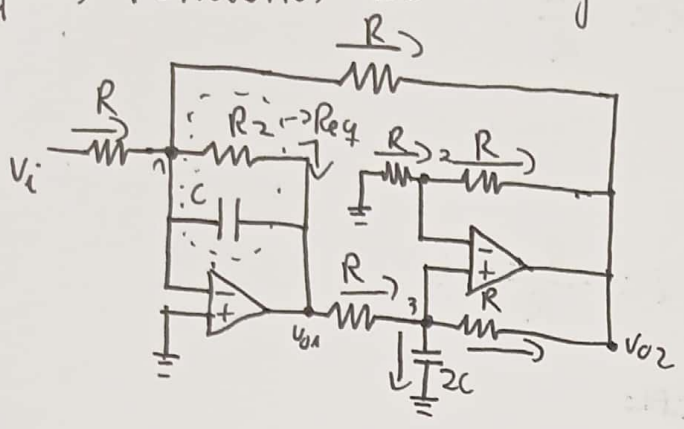
$$\frac{V-0}{R_1} + \frac{V-V_0}{R_2} \mp I_N = 0$$

$$V \left(\frac{1}{R_1} + \frac{1}{R_2} \right) \pm I_N = \frac{V_0}{R_2} \rightarrow \frac{V_0}{R_2} = \pm I_N \mp I_N R \left(\frac{1}{R_1} + \frac{1}{R_2} \right) - I_P R' \left(\frac{1}{R_1} + \frac{1}{R_2} \right)$$

$$V_0 = \pm I_N \left(R_2 + \frac{R R_2}{R_1} + R \right) - I_P R' \left(\frac{R_2}{R_1} + 1 \right)$$

$$R_2 + \frac{RR_2}{R_1} + R = R' \left(\frac{R_2}{R_1} + 1 \right) \rightarrow R' = \frac{R_1 R_2 + R R_2 + R R_1}{R_2 + R_1}$$

3 | a) Funciones de transf.



$$R_{eq} = \frac{1}{\frac{1}{R_2} + Cs} = \frac{R_2}{1 + R_2 Cs}$$

$$1 \quad \frac{V_i - 0}{R} = \frac{0 - V_{01}}{R_{eq}} + \frac{0 - V_{02}}{R} \rightarrow \frac{V_i}{R} = -\frac{V_{01}}{R_{eq}} - \frac{V_{02}}{R} = -\left(\frac{R Cs}{R_{eq}} + \frac{1}{R} \right) V_{02} *$$

$$2 \quad \frac{0 - V}{R} = \frac{V - V_{02}}{R} \rightarrow V = \frac{V_{02}}{2}$$

$$3 \quad \frac{V_{01} - V}{R} = \frac{V - 0}{\frac{1}{2Cs}} + \frac{V - V_{02}}{R} \rightarrow \frac{V_{01}}{R} = V \left(2Cs + \frac{2}{R} \right) - \frac{V_{02}}{R} = V_{02} \left(Cs + \frac{1}{R} \right) - \frac{V_{02}}{R}$$

$$V_{01} = R Cs V_{02}$$

$$\begin{aligned} * \quad V_i &= - \left(\frac{R^2 Cs}{R_{eq}} + 1 \right) V_{02} = - \left(\frac{R^2 Cs (1 + R_2 Cs)}{R_2} + 1 \right) V_{02} = \\ &= - \left(\frac{R^2 Cs + R^2 R_2 C^2 S^2 + R_2}{R_2} \right) V_{02} = - \left(\frac{S^2 + \frac{R^2 Cs}{R^2 R_2 C} + \frac{R_2}{R^2 R_2 C^2}}{\frac{R_2}{R^2 R_2 C^2}} \right) V_{02} = \\ &= - \left(\frac{S^2 + \frac{S}{R_2 C} + \frac{1}{R^2 C^2}}{\frac{1}{R^2 C^2}} \right) V_{02} \rightarrow \frac{V_{02}}{V_i} = \frac{-\frac{1}{R^2 C^2}}{S^2 + \frac{1}{R_2 C} S + \frac{1}{R^2 C^2}} = G_2 \quad \text{Pasa bajo} \end{aligned}$$

Sust. V_{02} por $\frac{V_{01}}{R Cs}$

$$\frac{V_{01}}{V_i} = \frac{-\frac{1}{R C} S}{S^2 + \frac{1}{R_2 C} S + \frac{1}{R^2 C^2}} = G_1 \quad \text{Pasa banda}$$

obtenemos seis parámetros

$$G_2 = \frac{H_0 \omega_0^2}{s^2 + \frac{\omega_0}{Q}s + \omega_0^2} \left\{ \begin{array}{l} -\omega_0^2 = \sqrt{\frac{1}{R^2 C^2}} = \frac{1}{RC} \omega_c \\ -H_0 \omega_0^2 = -\frac{1}{R^2 C^2} \rightarrow H_0 = -1 \\ \frac{\omega_0}{Q} = -\frac{1}{RC} \rightarrow Q = \frac{R_2}{R} \end{array} \right.$$

$$G_1 = \frac{\frac{H_0 \omega_0}{Q} s}{s^2 + \frac{\omega_0}{Q}s + \omega_0^2} \left\{ \begin{array}{l} -\omega_0 = \frac{1}{RC} \\ -Q = \frac{R_2}{R} \\ -\frac{H_0 \omega_0}{Q} = \frac{1}{RC} \rightarrow -Q = -\frac{R_2}{R} = H_0 \end{array} \right.$$

b) $C = 1 \text{ nF}$, $R = 15'8 \text{ k}\Omega$, $R_2 = 80'6 \text{ k}\Omega$

$$\omega_0 = 63297'13 \text{ Hz} \rightarrow f_0 = 10073'04 \text{ Hz}$$

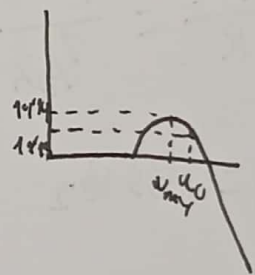
$$Q = 5'101 \quad H_{01} = -Q = -5'101$$

$$H_{02} = -1$$

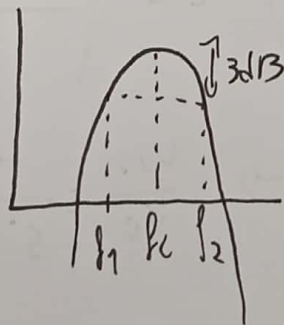
62 $\omega_{\text{max}} = \omega_0 \sqrt{1 - \frac{1}{2Q^2}} = 62680'14 \text{ Hz}$

$$20 \log_{10} |G(j\omega_{\text{max}})| = 20 \log_{10} \left| \frac{H_0 Q}{\sqrt{1 - \frac{1}{4Q^2}}} \right| = 14'19 \text{ dB}$$

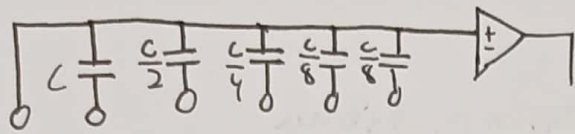
$$20 \log_{10} |G(j\omega_0)| = 20 \log_{10} |H_0 Q| = 14'25 \text{ dB}$$



61 $BW = f_2 - f_1 = \frac{f_0}{Q}$ $\left\{ \begin{array}{l} f_1^2 + \frac{f_0}{Q} f_1 - f_0^2 = 0 \\ f_1 \cdot f_2 = f_0^2 \end{array} \right. \left\{ \begin{array}{l} f_1 = 9134'81 \text{ Hz} \\ f_2 = \frac{f_0^2}{f_1} = 11107'74 \text{ Hz} \end{array} \right.$

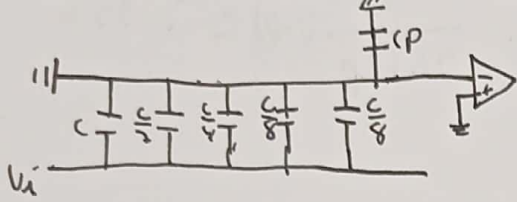


4] ADC redist. de carga $n=4$, $V_{ref}=3V$, $C=8pF$, $C_p=4pF$, $v_i=1.8V$ PSF ³



3 ciclos | muestreo
retención
redistribución

- Ciclo de muestreo \rightarrow todos los cond. a tierra por arriba y a v_i por abajo

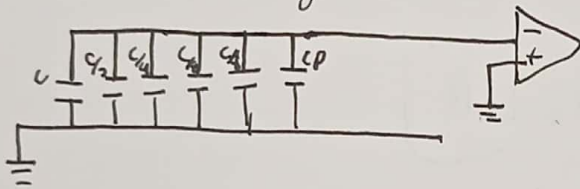


$$Q_1 = v_i C_{eq} \quad \text{con } C_{eq} = \sum C = 2C$$

C_p no importa aquí

- Ciclo de retención

Abrimos sw y los cond a tierra



C_p continúa

la carga debe conservarse

$$Q_1 = Q_p \rightarrow 2Cv_i = -V_p(2C + C_p)$$

$$V_p = -\frac{2C}{2C + C_p} v_i = -1.44V$$

- Ciclo de redistribución de carga

- Conectamos C a V_{ref} y el resto a tierra

$$(V_{ref} - V_1)C = C_{eq}V_1 \rightarrow V_1 = \frac{C}{2C + C_p} V_{ref} = 1.2$$

$$V_1 + V_p = 1.2 - 1.44 = -0.24 < 0 \quad b_3 = 1$$

- Conectamos C y $\frac{C}{2}$ a V_{ref} y el resto a tierra

$$(V_{ref} - V_2)(C + \frac{C}{2}) = (\frac{C}{4} + \frac{2C}{8} + C_p)V_2 \rightarrow V_2 = \frac{C + \frac{C}{2}}{2C + C_p} V_{ref} = 1.8$$

$$V_2 + V_p = 1.8 - 1.44 = 0.36 > 0 \quad b_2 = 0$$

- Conectamos C y $\frac{C}{4}$ a V_{ref} y el resto a tierra

$$(V_{ref} - V_3)(C + \frac{C}{4}) = (\frac{C}{2} + \frac{2C}{8} + C_p)V_3 \rightarrow V_3 = \frac{C + \frac{C}{4}}{2C + C_p} V_{ref} = 1.5V$$

$$V_3 + V_p = 1'5 - 1'44 = 0'06 > 0 \quad b_1 = 0$$

Por ultimo

Conectamos $C_y \frac{C}{8}$ a V_{ref} y el resto a tierra

$$(V_{ref} - V_n) \left(C + \frac{C}{8} \right) = \left(\frac{C}{2} + \frac{C}{4} + \frac{C}{8} \right) V_4 \rightarrow V_4 = \frac{C + \frac{C}{8}}{2C + C_p} V_{ref} = 1'35 V$$

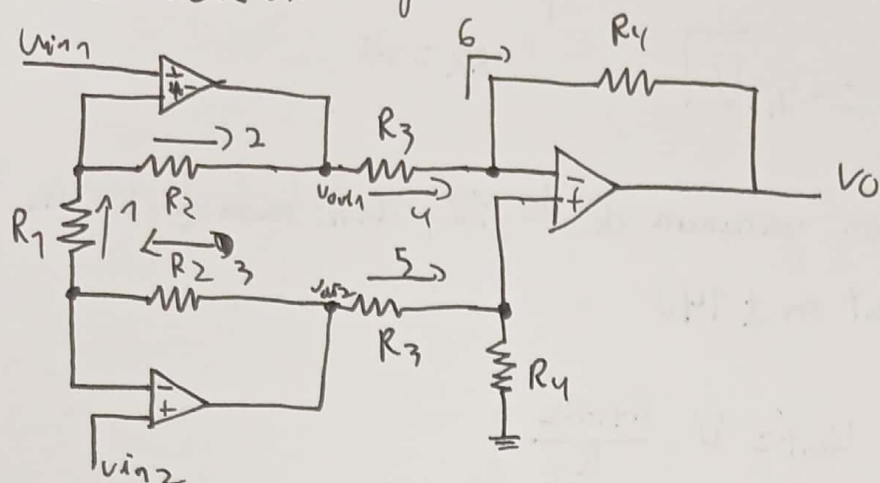
$$V_4 + V_p = -404 \quad \text{da} \quad b_0 = 1$$

Código de salida $b_3 b_2 b_1 b_0 = 1001$

$$V_o = V_{ref} \left(\frac{1}{2} + \frac{1}{16} \right) = 1'6875 V$$

$$\text{Error } E = \frac{V_o - V_i}{V_{LSB}} = \frac{1'6875 - 1'8}{3/24} = -0'6 \text{ LSB}$$

1] Ganancia en modo común, diferencial y factor de rechazo en cada una y el total



1^{ra} etapa

$$\frac{v_{o2} - v_{i1}}{R_1} = \frac{v_{i1} - v_{o1}}{R_2} \rightarrow v_{o1} = R_2 \left[\frac{v_{i1}}{R_2} + \frac{v_{i1}}{R_1} - \frac{v_{i2}}{R_1} \right]$$

$$\frac{v_{o1} - v_{i2}}{R_2} = \frac{v_{i2} - v_{i1}}{R_1} \rightarrow v_{o2} = R_2 \left[\frac{v_{i2}}{R_2} + \frac{v_{i2}}{R_1} - \frac{v_{i1}}{R_1} \right]$$

$$v_{out} = A_d v_d + A_{cm} v_{cm} \left\{ \begin{array}{l} A_d = v_{i2} - v_{i1} \\ A_{cm} = \frac{(v_{i2} + v_{i1})}{2} \end{array} \right.$$

Diferencial $v_{o2} - v_{o1} = (v_{i2} - v_{i1}) \left(1 + 2 \frac{R_2}{R_1} \right) \rightarrow A_{d1} = 1 + 2 \frac{R_2}{R_1} = 11 \text{ V/V}$

Modo común $\frac{v_{o2} + v_{o1}}{2} = \frac{v_{i1} + v_{i2}}{2} \cdot 1 \rightarrow A_{cm1} = 1$

$$CMRR_1 = 20 \log_{10} \frac{A_{d1}}{A_{cm1}} = 20,83 \text{ dB}$$

2^a etapa

$$\frac{v_{o1} - v}{R_3} = \frac{v - v_0}{R_4}$$

$$\frac{v_{o2} - v}{R_3} = \frac{v - 0}{R_4} \rightarrow v = v_{o2} \frac{R_4}{R_3 + R_4}$$

$$v_{out} = (v_{o2} - v_{o1}) \frac{R_4}{R_3} \left\{ \begin{array}{l} \text{Parámetro} \\ \text{diferencial} \end{array} \right.$$

$$A_{d2} = \frac{R_4}{R_3} = 2 \text{ V/V}$$

$$A_{cm2} = 0$$

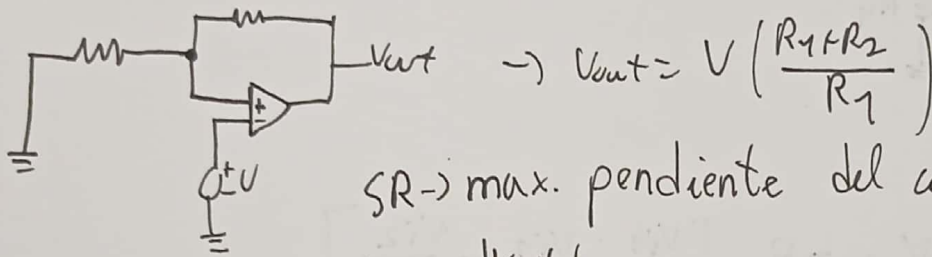
$$CMRR_2 = 20 \log_{10} \left(\frac{2}{0} \right) = \infty$$

Para el total sustituyamos V_{i2} y V_{i1}

$$V_{out} = \left[(V_{i2} - V_{i1}) \left(1 + 2 \frac{R_2}{R_1} \right) \right] \frac{R_4}{R_3} = \begin{cases} A_d = \left(1 + 2 \frac{R_2}{R_1} \right) \frac{R_4}{R_3} = 22 \text{ V/V} \\ A_{CM} = 0 \end{cases}$$

$$\left[V_{out} = 22 (2,25 - 2,4) = -3,5 \text{ V} \right] \quad \text{CMRR} = \infty$$

2] AO a $\pm 15 \text{ V}$ (no inv.) con ganancia de 10 V/V , ancho banda $f_f = 1,5 \text{ MHz}$
 Respuesta $S = 0,8 \frac{\text{V}}{\mu\text{s}}$ y sat en $\pm 14 \text{ V}$



SR \rightarrow max. pendiente del cambio posible para la salida

$$SR = \left. \frac{dV_{out}}{dt} \right|_{\max} = V_{\max} \cdot \omega$$

Ancho de Banda $\rightarrow BW = f_f \beta = \frac{f_f}{\text{ganancia}} = 150 \text{ kHz}$ no se puede superar.

a) $V_{out} = A_d V_{in} = 10 \cdot 0,6 = 6 \text{ V} < V_{\max} \checkmark$

$$SR = \omega V = 2\pi f V \rightarrow f = \frac{SR}{2\pi V} = \frac{0,8 \cdot 10^6}{2\pi \cdot 6} = 21,22 \text{ kHz} < BW \checkmark$$

b) $f = 10 \text{ kHz} \rightarrow V = \frac{SR}{2\pi f} = 1,273 \text{ V} < V_{\max} \checkmark$

$$V_{\text{in max}} = \frac{1,273}{10} = 0,1273 \text{ V}$$

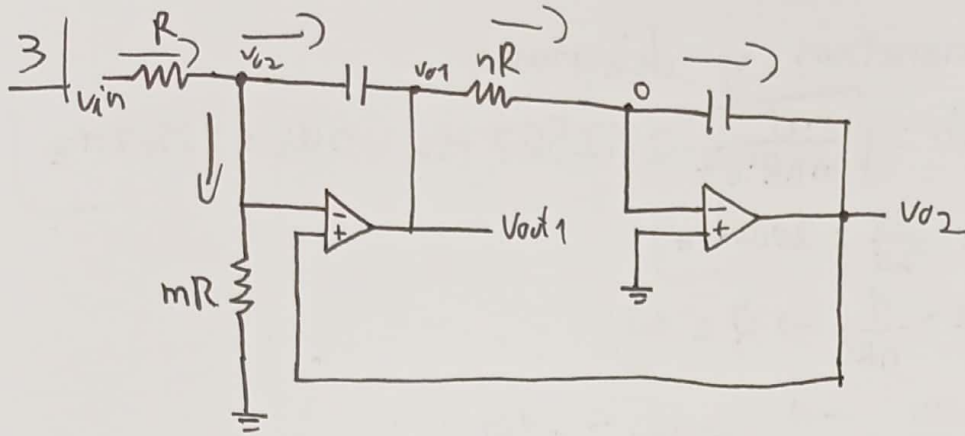
c) $V_{in} = 50 \text{ mV} \rightarrow V_{out} = 10 \cdot 50 \times 10^{-3} = 0,5 \text{ V} < V_{\text{out max}} \checkmark$

$$f = \frac{SR}{2\pi V} = 254 \text{ kHz} > BW \quad \text{El rango ser\u00eda hasta BW}$$

d) $V_{\max} = \frac{SR}{2\pi f} = \frac{0,8 \cdot 10^6}{2\pi \cdot 5 \cdot 10^3} = 25 \text{ V} > V_{\text{out max}} \quad \text{rango hasta } +15 \text{ V}$

$f = 5 \text{ kHz}$

$V_{in} = \frac{15}{10} = 1,5 \rightarrow \text{rango util de } 0 \rightarrow 1,5 \text{ V}$



$$(1) \frac{V_{in} - V_{o2}}{R} = \frac{V_{o2} - 0}{mR} + \frac{V_{o2} - V_{o1}}{1/Cs}$$

$$(2) \frac{V_{o1} - 0}{nR} = \frac{0 - V_{o2}}{1/Cs} \rightarrow V_{o1} = -nRCs V_{o2}$$

Despejamos 1 $\frac{V_{in}}{R} = V_{o2} \left(\frac{1}{mR} + \frac{1}{R} + Cs \right) - V_{o1}Cs$

$$V_{in} = V_{o2} \left(\frac{1}{m} + 1 + RCs \right) - V_{o1}RCs =$$

$$= V_{o2} \left(\frac{1}{m} + 1 + RCs + nR^2C^2s^2 \right) = V_{o2} \left(\frac{1+m + mRCs + mR^2C^2ns^2}{m} \right) =$$

$$= V_{o2} \left(\frac{\frac{1+m}{mR^2C^2} + \frac{RC}{nR^2C^2}s + s^2}{\frac{1}{nR^2C^2}} \right) = \left(\frac{s^2 + \frac{1}{nRC}s + \frac{1+m}{mR^2C^2}}{\frac{1}{nR^2C^2}} \right) V_{o2}$$

$$G_2 = \frac{V_{o2}}{V_{in}} = \frac{\frac{1}{nR^2C^2}}{s^2 + \frac{1}{nRC}s + \frac{1+m}{mR^2C^2}}$$

Pasa baja

$$G_1 = \frac{V_{o1}}{V_{in}} = \frac{-\frac{V_{o1}}{nRCs}}{s^2 + \frac{1}{nRC}s + \frac{1+m}{mR^2C^2}}$$

Pasa banda

Calcularemos sus parámetros y diagramas

$$G_1 = \frac{H_0 \omega_0}{s^2 + \frac{\omega_0}{Q}s + \omega_0^2}$$

$$\omega_0 = \sqrt{\frac{m+1}{m} R^2 C^2} = 12567 \text{ Hz} \rightarrow \omega_0 = 12567 \text{ Hz}$$

$$f_0 = \frac{\omega_0}{2\pi} = 2000 \text{ Hz}$$

$$\frac{\omega_0}{Q} = \frac{1}{nRC} \rightarrow Q = 10$$

$$\frac{H_0 \omega_0}{Q} = \frac{-1}{RC} \rightarrow H_0 = -100$$

Para el diagrama $BW = \frac{f_0}{Q} = f_2 - f_1 = 200$

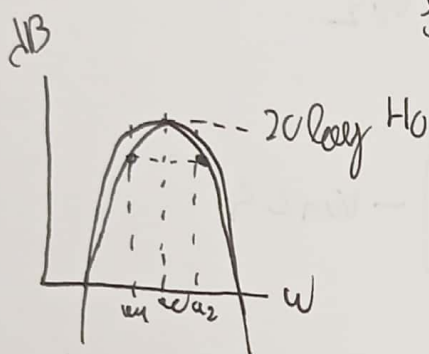
$$f_0^2 = f_1 \cdot f_2$$

$$f_1^2 + \frac{f_0}{Q} f_1 - f_0^2 = 0$$

$$\hookrightarrow f_1 = 1902 \text{ Hz}$$

$$\downarrow$$

$$f_2 = 2103 \text{ Hz}$$



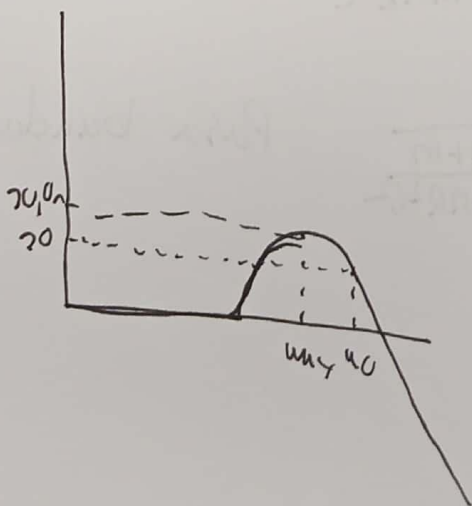
G_2 ω_0, f_0, Q iguales

$$H_0 \omega_0^2 = \frac{1}{nR^2 C^2} \rightarrow |H_0| = 1$$

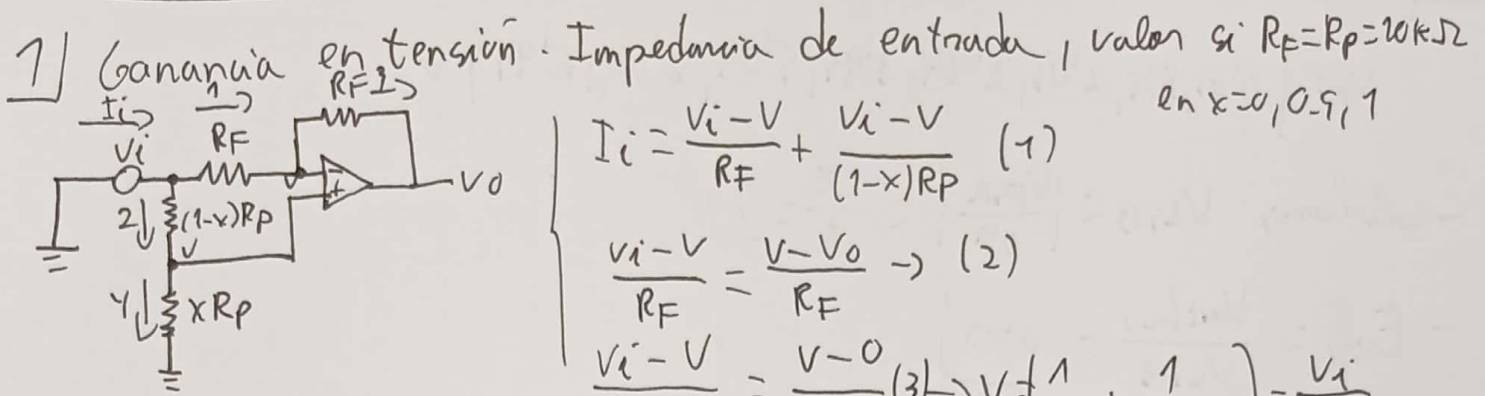
$$\omega_{max} = \omega_0 \sqrt{1 - \frac{1}{4Q^2}} = 12535 \text{ Hz}$$

$$20 \log_{10} |G(\omega_{max})| = 20 \log_{10} \left| \frac{Q H_0}{\sqrt{1 - \frac{1}{4Q^2}}} \right| = 20,01 \text{ dB}$$

$$20 \log_{10} |G(\omega_0)| = 20 \log_{10} |H_0 Q| = 20 \text{ dB}$$



Julio 2020



$$I_i = \frac{V_i - V}{R_F} + \frac{V_i - V}{(1-x)R_P} \quad (1)$$

$$\frac{V_i - V}{R_F} = \frac{V - V_O}{R_F} \rightarrow (2)$$

$$\frac{V_i - V}{(1-x)R_P} = \frac{V - 0}{xR_P} \quad (3) \rightarrow V = \left[\frac{1}{xR_P} + \frac{1}{(1-x)R_P} \right]^{-1} \frac{V_i}{(1-x)R_P}$$

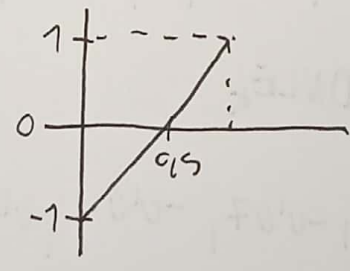
Sust. 3 en 2 $\frac{V_i - x V_i}{R_F} = \frac{x V_i - V_O}{R_F}$

$\hookrightarrow V = x V_i$

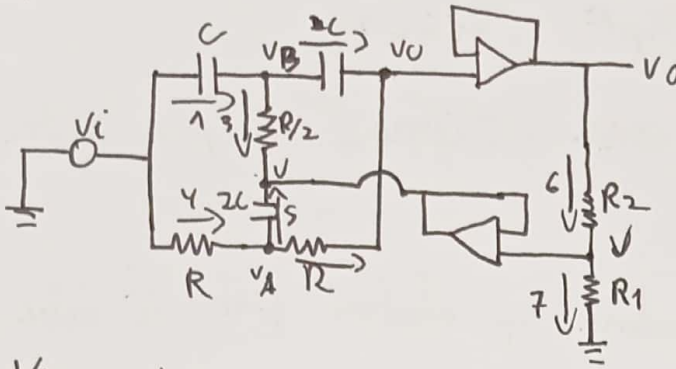
$V_i(1 - 2x) = V_O \rightarrow V_O = A_d V_i \rightarrow \boxed{A_d = 1 - 2x}$ Ganancia en tensión

1) $I_i = (V_i - V) \left(\frac{1}{R_F} + \frac{1}{(1-x)R_P} \right) = V_i(1-x) \left(\frac{1}{R_F} + \frac{1}{(1-x)R_P} \right) =$
 $= V_i \left(\frac{(1-x)}{R_F} + \frac{1}{R_P} \right) = V_i \left(\frac{(1-x)R_P + R_F}{R_F R_P} \right) = V_i \left(\frac{R[(1-x)+1]}{R^2} \right) =$
 $= V_i \left(\frac{2-x}{R} \right) \rightarrow \boxed{R_i = \frac{V_i}{I_i} = \frac{R}{2-x}}$

- $Z_i(0) = 5\text{k}\Omega$
- $Z_i(0.5) = 6.67\text{k}\Omega$
- $Z_i(1) = 10\text{k}\Omega$



2 | parametros y Bode



$$v_i - v_B = \frac{v_B - v_0}{1/c_s} = \frac{v_B - v}{R/2} \quad (1)$$

$$v_i - v_A = \frac{v_A - v_0}{R} = \frac{v_A - v}{1/2c_s} \quad (2)$$

$$v_0 - v = \frac{v - 0}{R_1} \quad (3)$$

$$\frac{v_B - v}{R/2} = \frac{v_A + v}{1/2c_s} = 0 \quad (4) \quad \frac{v_A - v_0}{R} + \frac{v_B - v_0}{1/c_s} = 0$$

$$-\frac{v_0}{R_2} = v \left(\frac{1}{R_1} + \frac{1}{R_2} \right) \Rightarrow v_0 = v \left(\frac{R_2}{R_1} + 1 \right)$$

$$v = \frac{v_0}{\left(\frac{R_2}{R_1} + 1 \right)}$$

- Despejando (1) y sust. v obtenemos $v_B = \frac{c_s}{2(c_s + \frac{1}{R})} v_i + \frac{c_s + \frac{2}{R}}{2(c_s + \frac{1}{R})} \frac{1}{1 + \frac{R_2}{R_1}} v_0$

- Despejando (2) y sust. v $v_A = \frac{1}{R(2c_s + \frac{2}{R})} v_i + \frac{1}{2c_s + \frac{2}{R}} \frac{1 + \frac{R_2}{R_1}}{2c_s} v_0$

- Remix juntando todo en 4 y despejando $\frac{v_0}{v_i}$

$$\frac{v_0}{v_i} = \frac{s^2 + \frac{1}{(RC)^2}}{s^2 + \frac{4}{RC} \frac{R_2}{R_1 + R_2} s + \frac{1}{(RC)^2}} \quad \text{banda eliminada}$$

- Calculo de parametros

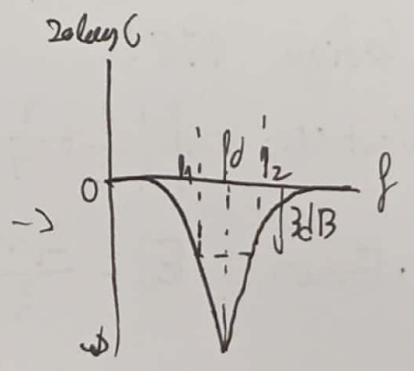
$$\omega_0 = \frac{1}{RC} = 374,47 \text{ rad/s} \rightarrow f_0 = 59,05 \text{ Hz}$$

$$\frac{\omega_0}{\alpha} = \frac{4}{RC} \frac{R_2}{R_1 + R_2} \rightarrow \alpha = \frac{R_1 + R_2}{4R_2} = 5$$

$$H_0 = 1$$

- Calculo f_{p1} y f_{p2}

$$f_2 - f_1 = \frac{f_0}{\alpha} \quad \left\{ \begin{array}{l} f_1^2 + \frac{f_0}{\alpha} f_1 - f_0^2 = 0 \\ f_0^2 = f_1 f_2 \end{array} \right. \quad \left\{ \begin{array}{l} f_1 = 49,29 \text{ Hz} \\ f_2 = 59,30 \text{ Hz} \end{array} \right.$$



3] ADC redist. de carga

$$n=4 \quad V_{ref}=3V \quad C=8pF \quad C_p=4pF \quad V_i=2.5V$$

- Ciclo de muestreo: todos los cond. a tierra y C_p no afecta

$$Q = V_i \cdot C_{eq} = 2C V_i$$

- Ciclo de retención: abrimos SW, ahora C_p afecta pero Q debe mantenerse

$$Q_1 = Q_2 \rightarrow 2C V_i = -V_p (2C + C_p) \rightarrow V_p = -\frac{2C}{2C + C_p} V_i = -2V$$

- Ciclo de redist. de carga: Vamos abriendo poniendo a V_{ref} o tierra para cada bit.

• C a V_{ref}
resto a tierra

$$(V_{ref} - V_1)C = (C + C_p)V_1 \rightarrow V_1 = \frac{C}{2C + C_p} V_{ref} = 1.5V$$

$$V_p + V_1 = -1 < 0 \rightarrow \boxed{b_3 = 1}$$

• C y $\frac{C}{2}$ a V_{ref}
resto tierra

$$(V_{ref} - V_2)(C + \frac{C}{2}) = (\frac{C}{4} + C_p)V_2 \rightarrow V_2 = \frac{C + \frac{C}{2}}{2C + C_p} V_{ref} = 1.8V$$

$$V_p + V_2 = -0.5 < 0 \rightarrow \boxed{b_2 = 1}$$

• C y $\frac{C}{2}$ y $\frac{C}{4}$ a V_{ref}

$$(V_{ref} - V_3)(C + \frac{C}{2} + \frac{C}{4}) = (\frac{2C}{8} + C_p)V_3 \rightarrow V_3 = \frac{(C + \frac{C}{2} + \frac{C}{4})}{2C + C_p} V_{ref} = 2.1V$$

$$V_p + V_3 = +0.1 > 0 \rightarrow b_1 = 0$$

• C , $\frac{C}{2}$ y $\frac{C}{8}$ a V_{ref}

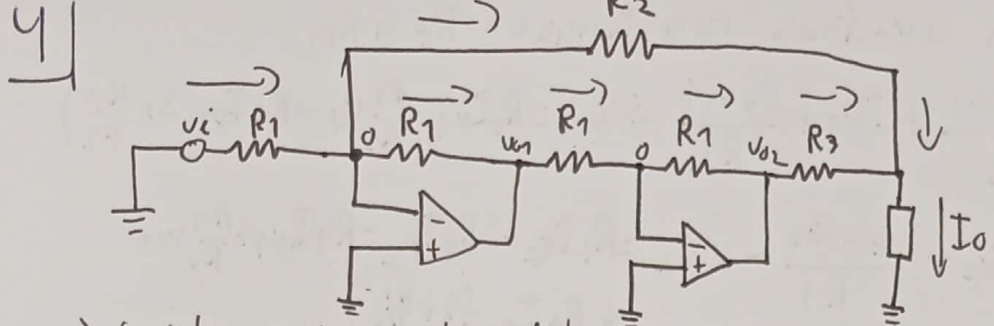
$$(V_{ref} - V_4)(C + \frac{C}{2} + \frac{C}{8}) = (\frac{C}{4} + \frac{C}{8} + C_p)V_4 \rightarrow V_4 = \frac{(C + \frac{C}{2} + \frac{C}{8})}{2C + C_p} V_{ref} = 2.34V$$

$$V_p + V_4 = -0.05 < 0 \rightarrow b_0 = 1$$

• Código 1101

$$V_{out} V_C = V_{ref} \left(\frac{1}{2} + \frac{1}{4} + \frac{0}{8} + \frac{1}{16} \right) = 2.44V$$

• Error $E_C = \frac{2.44 - 2.5}{3/2} = -0.134LSB$



a) Corriente y resistencia de salida, condición resistencia infinita

$$-\frac{v_i - 0}{R_1} = \frac{0 - v_0}{R_2} + \frac{0 - v_{01}}{R_1} \rightarrow v_{01} = -v_i - \frac{R_1}{R_2} v_0$$

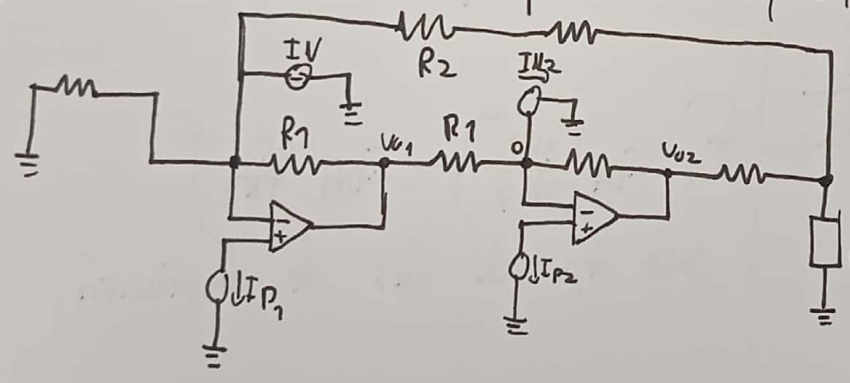
$$-\frac{v_{01} - 0}{R_1} = \frac{0 - v_{02}}{R_1} \rightarrow v_{01} = -v_{02} \rightarrow v_{02} = v_{01} + \frac{R_1}{R_2} v_0$$

$$-\frac{v_{02} - v_0}{R_3} = \frac{0 - v_0}{R_2} + I_0 \rightarrow \frac{v_{02}}{R_3} = v_0 \left(\frac{1}{R_3} - \frac{1}{R_2} \right) + I_0$$

$$I_0 = \frac{v_i}{R_3} + \left(\frac{R_1}{R_2 R_3} - \frac{1}{R_2} - \frac{1}{R_3} \right) v_0 \rightarrow R_0 = \frac{1}{\frac{R_1}{R_2 R_3} - \frac{1}{R_2} - \frac{1}{R_3}} = \frac{R_2 R_3}{R_1 - (R_2 + R_3)}$$

Cond. $R_0 \rightarrow \infty \rightarrow R_1 = R_2 + R_3$

b) añadimos corrientes de polarización, v_1 a tierra



Las corrientes I_{N1} e I_{N2} siempre dirección a la tierra

Las corrientes I_p no contribuyen I_0 debido a que no entra corriente por + así que está entre 2 tierras

$$I_{N1} - \frac{v_{01}}{R_1} = \frac{v_0}{R_2} = 0 \rightarrow v_{01} = R_1 I_{N1} - \frac{R_1}{R_2} v_0$$

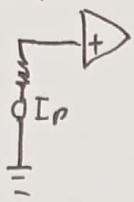
$$\frac{v_{01}}{R_1} = I_{N2} - \frac{v_{02}}{R_1} \rightarrow v_{02} = R_1 (I_{N2} - I_{N1}) + \frac{R_1}{R_2} v_0$$

$$\frac{v_{02} - v_0}{R_3} = I_0 + \frac{v_0}{R_2} \rightarrow I_0 = \frac{R_1}{R_3} (I_{N2} - I_{N1}) + v_0 \left(\frac{R_1}{R_2 R_3} - \frac{1}{R_2} - \frac{1}{R_3} \right)$$

$$I_0 = \frac{R_1}{R_3} (I_{N2} - I_{N1})$$

$R_0 \rightarrow \infty$

c) Ahora a las I_p les añadimos resistencias R_A y R_B



$$\frac{V_A}{R_1} = \frac{V_A - V_{01}}{R_1} + I_{N1} + \frac{V_A - V_0}{R_2} \rightarrow V_{01} = R_1 I_{N1} - \frac{R_1}{R_2} V_0 - R_A I_{P1} (2 + \frac{R_1}{R_2})$$

$$\frac{V_{01} - V_B}{R_1} = I_{N2} + \frac{V_B - V_{02}}{R_1} \rightarrow V_{02} = R_1 I_{N2} - 2R_B I_{P2} - R_1 I_{N1} + \frac{R_1}{R_2} V_0 + R_A I_{P1} (2 + \frac{R_1}{R_2})$$

$$\frac{V_{02} - V_0}{R_3} + \frac{V_A - V_0}{R_2} = I_0 \rightarrow I_0 = I_{P1} R_A \left(\frac{2}{R_3} + \frac{R_1}{R_2 R_3} + \frac{1}{R_2} \right) - \frac{2R_B}{R_3} I_{P2} +$$

$$V_A = -R_A I_{P1} + \frac{R_1}{R_3} (I_{N2} - I_{N1})$$

$$V_B = -R_B I_{P2}$$

Ahora escogí R_A y R_B de forma que anule $I_{pi} = \frac{I_{Ni} + I_{Pi}}{2}$

$$I_0 = \frac{I_{PA}}{2} \left[R_A \left(\frac{2}{R_3} + \frac{R_1}{R_2 R_3} - \frac{1}{R_3} \right) \right] + \frac{I_{PB}}{2} \left[\frac{R_1}{R_3} - \frac{2R_B}{R_3} \right] + I_{0A} \left[R_A \left(\frac{2}{R_3} + \frac{R_1}{R_2 R_3} - \frac{1}{R_3} \right) + \frac{R_1}{2R_2} \right]$$

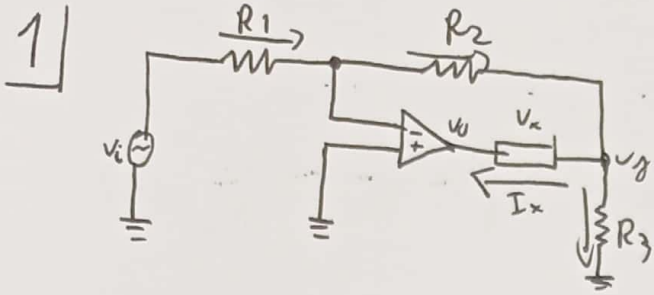
$$+ I_{0B} \left[-\frac{2R_B}{R_3} - \frac{R_1}{2R_2} \right] \quad \text{con} \quad I_0 = I_P - I_N \quad \left\{ \begin{array}{l} I_P = I_P + \frac{I_D}{2} \\ I_N = I_P - \frac{I_D}{2} \end{array} \right.$$

$$\bullet R_A = \frac{R_1/R_3}{2R_2 + R_1 - R_2} = \frac{R_1 R_2}{R_1 + R_2}$$

$$\bullet R_B = \frac{R_1}{2}$$

$$\left(I_0 = I_{0A} \left[\frac{3R_1}{2R_3} \right] - I_{0B} \frac{3R_1}{2R_2} \right)$$

solo dep. de las de desviación



- No ideal $v_o = (v_+ - v_-) A = -A v_-$
- Queremos $z = \frac{v_x}{I_x}$
- $v_x = v_y - (-A v_-) \rightarrow v_y = -A v_- + v_x$
- Ponemos $v_i = 0$

$$\frac{0 - v_-}{R_1} = \frac{v_- - v_y}{R_2} \rightarrow v_y = v_- \left(\frac{R_1 + R_2}{R_2} \right) \rightarrow v_- = v_y \left(\frac{R_2}{R_1 + R_2} \right)$$

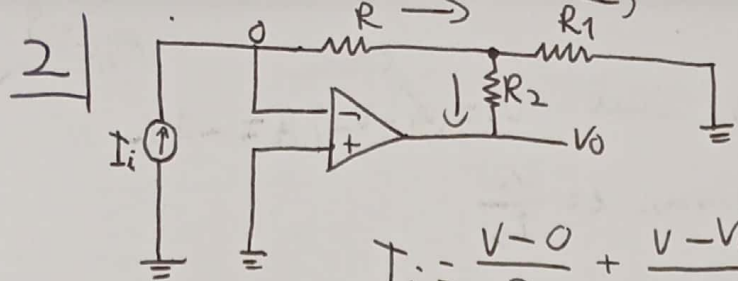
$$\frac{v_- - v_y}{R_2} = I_x + \frac{v_y - 0}{R_3} \rightarrow I_x = \frac{v_-}{R_2} - v_y \left(\frac{R_2 + R_3}{R_2 R_3} \right)$$

$$I_x = v_y \left(\frac{R_2}{R_2(R_1 + R_2)} \right) - v_y \left(\frac{R_2 + R_3}{R_2 R_3} \right) = v_y \left(\frac{R_2}{R_2(R_1 + R_2)} - \frac{R_2 + R_3}{R_2 R_3} \right)$$

Cambiando v_y por v_x (me dio pereza y se lo copie a yayo).

$$I_x = \frac{v_x}{R_1(1 + A_d) + R_2} \left(\frac{R_2}{R_2} - \frac{(R_1 + R_2)(R_2 + R_3)}{R_2 R_3} \right)$$

$$z = \frac{v_x}{I_x} = \frac{R_3 R_2 [R_1(1 + A_d) + R_2]}{R_3 R_1 - (R_1 + R_2)(R_2 + R_3)} = -500 \text{ k}\Omega$$



a)

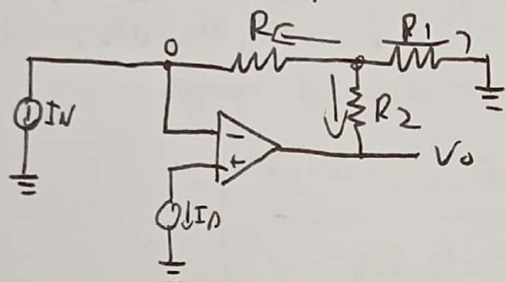
$$I_i = \frac{V-0}{R_1} + \frac{V-V_o}{R_2} \rightarrow I_i = \frac{-I_i R}{R_1} - \frac{I_i R}{R_2} - \frac{V_o}{R_2} \quad (1)$$

$$I_i = \frac{V_o - V}{R} \rightarrow V = -I_i R$$

$$(1) -I_i \left(1 + \frac{R}{R_1} + \frac{R}{R_2} \right) = \frac{V_o}{R_2} \rightarrow \left[V_o = -I_i \left(R_2 + \frac{R R_2}{R_1} + R \right) \right]$$

$$\frac{V_{out}}{I_i} = G = - \left(R_2 + \frac{R R_2}{R_1} + R \right)$$

b) Eliminamos I_i poniendo circuito abierto y añadimos I_N e I_p



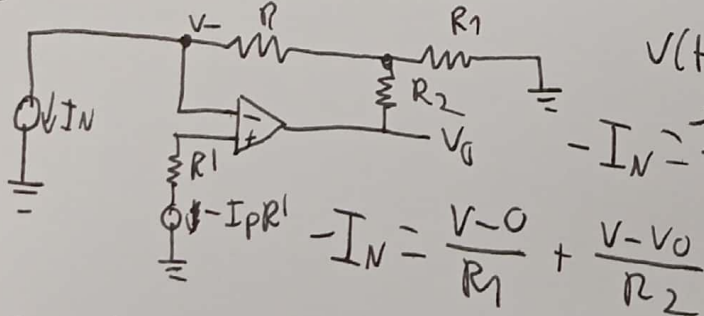
No puede entrar corriente en el operacional por lo que I_p no influye $V_- = 0$

$$-I_N = \frac{0-V}{R} \rightarrow V = +I_N R$$

$$-I_N = \frac{V-0}{R_1} + \frac{V-V_o}{R_2} \rightarrow \frac{V_o}{R_2} = I_N \left(1 + \frac{R}{R_1} + \frac{R}{R_2} \right)$$

$$V_o = I_N R_2 \left(1 + \frac{R}{R_1} + \frac{R}{R_2} \right)$$

c) Añadimos una resistencia R'



$$V(+) = V(-) = -I_p R'$$

$$-I_N = \frac{-I_p R' - V}{R} \quad (\text{veo que } I_N \text{ debería llevar un } - \text{ por la definición})$$

$$-I_N = \frac{V-0}{R_1} + \frac{V-V_o}{R_2}$$

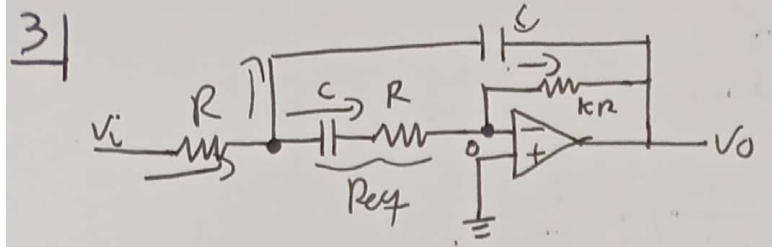
Sustituimos, despejamos V_o

$$V_o = I_N \left(R_2 + \frac{R R_2}{R_1} + R \right) - I_p \left(\frac{R' R_2}{R_1} + R \right)$$

$$\left(R_2 + \frac{R R_2}{R_1} + R \right) = \frac{R' R_2}{R_1} + R$$

Despejamos R'

$$R' = \frac{R_2 R_1 + R R_2 + R R_1}{R_2 + R_1}$$



$$R_{eq} = \frac{1}{Cs} + R = \frac{1+RCs}{Cs}$$

$$1) \frac{V_i - V}{R} = \frac{V - V_o}{1/Cs} + \frac{V - 0}{R_{eq}}$$

$$2) \frac{V - 0}{R_{eq}} = \frac{0 - V_o}{kR} \rightarrow V = -V_o \frac{R_{eq}}{kR} = -V_o \frac{1+RCs}{kRCs}$$

$$\frac{V_i}{R} = V \left(\frac{1}{R} + Cs + \frac{1}{R_{eq}} \right) - V_o Cs$$

$$V_i = V \left(1 + RCs + \frac{R}{R_{eq}} \right) - V_o RCs \rightarrow V_i = -V_o \left(\frac{1+RCs}{kRCs} \left(1 + RCs + \frac{R}{R_{eq}} \right) + RCs \right)$$

$$V_{in} = -V_o \left(\frac{(k+1)R^2C^2s^2 + 3RCs + 1}{kRCs} \right) = -V_o \left(\frac{s^2 + \frac{3}{(k+1)RC}s + \frac{1}{(k+1)R^2C^2}}{\frac{k}{(k+1)RC}s} \right)$$

$$\frac{V_o}{V_{in}} = G(s) = \frac{-\frac{k}{(k+1)RC}s}{s^2 + \frac{3}{(k+1)RC}s + \frac{1}{(k+1)R^2C^2}}$$

Pasa banda $G(s) = \frac{H_0 \omega_0 s}{s^2 + \frac{\omega_0}{Q}s + \omega_0^2}$

- Calculamos los parámetros

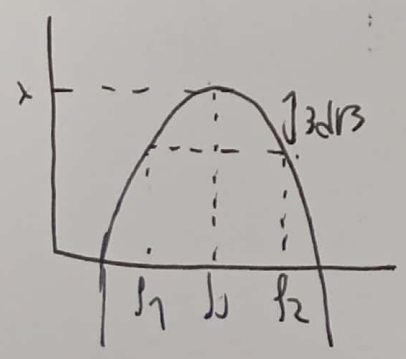
$$- \omega_0 = \sqrt{\frac{1}{k+1}} \frac{1}{RC} = 6298 \text{ rad/s} \rightarrow f_0 = 1002 \text{ Hz}$$

$$- \frac{\omega_0}{Q} = \frac{3}{(k+1)RC} \rightarrow Q = 5$$

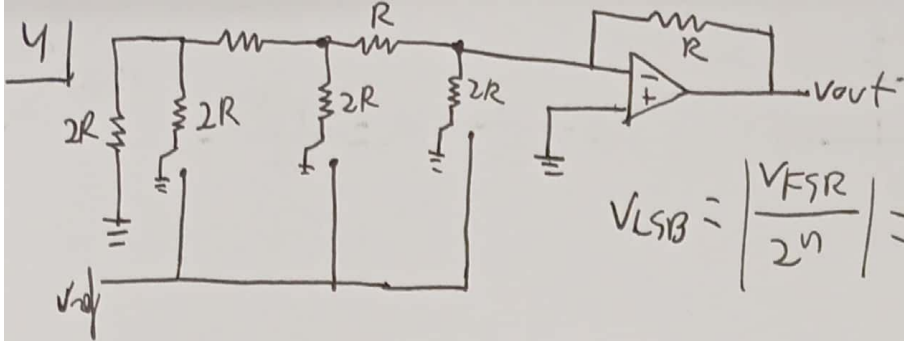
$$- \frac{H_0 \omega_0}{Q} = -\frac{k}{RC(k+1)} \rightarrow H_0 = -75$$

b) Diagrama $BW = \frac{f_0}{Q} = f_2 - f_1$ $f_1^2 + \frac{f_0}{Q} f_1 - f_0^2 = 0$ $f_2^2 = f_1 f_2$

$$\left. \begin{aligned} & f_1^2 + \frac{f_0}{Q} f_1 - f_0^2 = 0 \\ & f_2^2 = f_1 f_2 \end{aligned} \right\} \begin{cases} f_1 = 906.6 \text{ Hz} \\ f_2 = 1107 \text{ Hz} \end{cases}$$



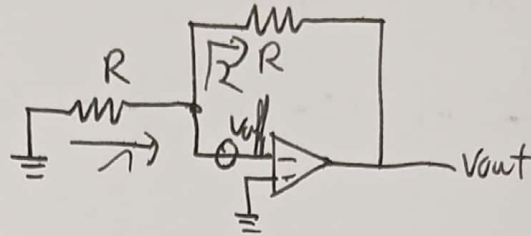
$$x = 20 \log_{10} |H_0| = 20 \log_{10} 75 \text{ dB}$$



$$V_{LSB} = \left| \frac{V_{FSR}}{2^n} \right| = \frac{1}{8}$$

- $E_{eff} = \frac{V_{out_{load}}}{V_{LSB}}$ Todos a tierra

Calculamos $R_{eq} = R \rightarrow$



$$V_0 = (V_+ - V_-) A_d = -V_- A_d$$

$$V_A = V_{eff} + V_- ; V_- = -\frac{V_0}{A_d}$$

$$I_1 = I_2$$

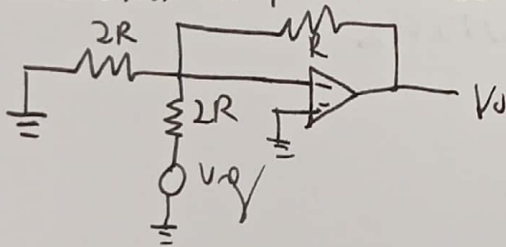
$$\frac{0 - V_A}{R} = \frac{V_A - V_{out}}{R} \rightarrow V_{out} = V_{eff} \left(2 - \frac{2}{A_d} \right)$$

Entonces $E_{eff} = \frac{V_{out_{load}}}{V_{LSB}} = 0.11 \text{ LSB}$

- Básicos calculos $E_g = \left(\frac{V_{out_{111}}}{V_{LSB}} - \frac{V_{out_{000}}}{V_{LSB}} \right) - (2^n - 1)$

Calculamos $V_{out_{111}} = V_{out}|_{100} + V_{out}|_{010} + V_{out}|_{001} + V_{out}|_{000}$

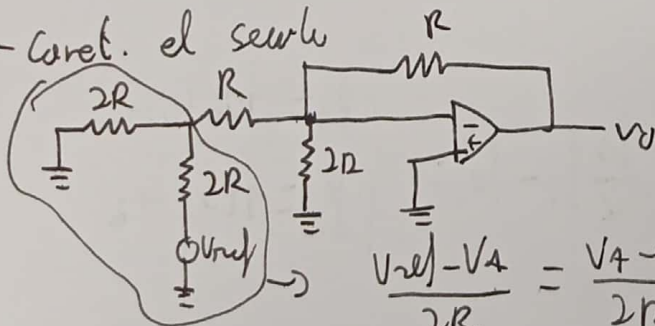
- Conectamos el primer a \$V_{ref}\$



$$\frac{V_{ref} - V_-}{2R} = \frac{V_- - 0}{2R} + \frac{V_- - V_{out}}{R}$$

$$L) V_{out}|_{100} = -\frac{A_d}{2(2+A_d)} \cdot V_{ref} = -\frac{100}{2(2+100)} \cdot 7 \cdot 10^{-3}$$

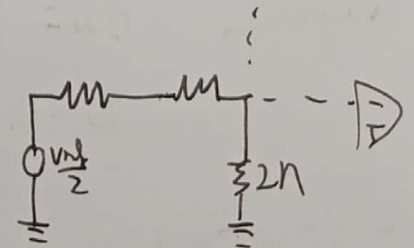
- Correc. el seculo



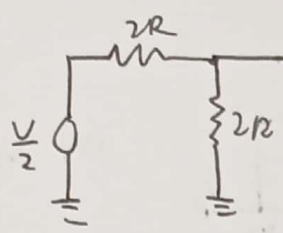
Se Hace Thevenin

$$\frac{V_{ref} - V_A}{2R} = \frac{V_A - 0}{2R} \rightarrow V_A = \frac{V_{ref}}{2}$$

$$Z_{eq} = \frac{1}{\frac{1}{2R} + \frac{1}{2R}} = R$$

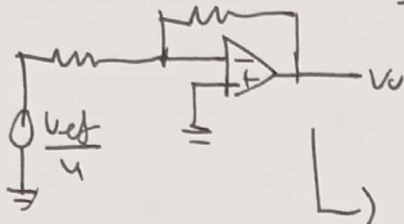


Repetimos theorem



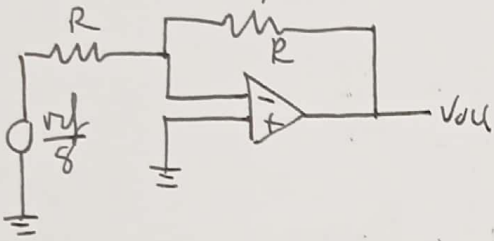
$$\frac{V_{ref} - V_A}{2R} = \frac{V_A}{2R}$$

$$\Rightarrow V_A = \frac{V_{ref}}{4}$$



$$\left. \right\} \frac{V_{ref} - v_-}{R} = \frac{v_- - v_{out}}{R} \rightarrow v_{out}|_{load} = -V_{ref} \frac{A_d}{4(2+A_d)}$$

- Por ultimo repetimos pero con la et resistora y haciendo theorem nos queda



$$\rightarrow \frac{V_{ref} - v_-}{R} = \frac{v_- - v_{out}}{R}$$

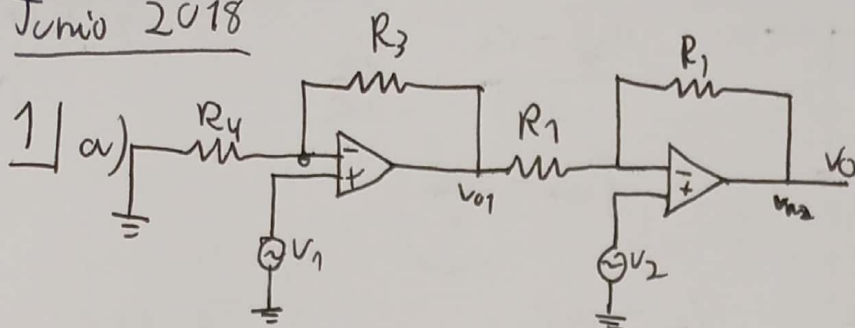
$$v_{out}|_{load} = -V_{ref} \left(\frac{A_d}{8(2+A_d)} \right)$$

Sumamos todo $\rightarrow V_{111} = 0,87V$

$$E_q = \left(\frac{V_{0111}}{V_{LSB}} - \frac{V_{0100}}{V_{LSB}} \right) \cdot (2^n - 1) = -0,19LSB$$

(No me gusta este ejercicio)

Junio 2018



a) $v_0 = A_d (v_2 - v_1)$

$$\frac{0 - v_1}{R_4} = \frac{v_1 - v_{01}}{R_3} \rightarrow \frac{v_{01}}{R_3} = v_1 \left(\frac{1}{R_4} + \frac{1}{R_3} \right) \rightarrow v_{01} = v_1 \left(\frac{R_3}{R_4} + 1 \right)$$

$$\frac{v_{01} - v_2}{R_1} = \frac{v_2 - v_0}{R_2} \rightarrow \frac{v_0}{R_2} = v_2 \left(\frac{1}{R_1} + \frac{1}{R_2} \right) - \frac{v_{01}}{R_1}$$

$$\hookrightarrow v_0 = v_2 \left(\frac{R_2}{R_1} + 1 \right) - \frac{R_2}{R_1} v_{01}$$

$$\hookrightarrow v_0 = v_2 \left(\frac{R_2}{R_1} + 1 \right) - v_1 \frac{R_2}{R_1} \left(\frac{R_3}{R_4} + 1 \right)$$

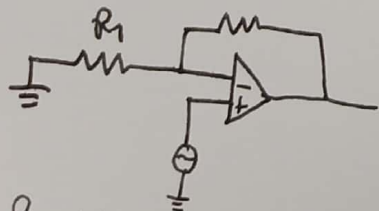
$$\frac{R_2}{R_4} + 1 = \frac{R_2}{R_1} \left(\frac{R_3}{R_4} + 1 \right) \rightarrow 1 + \frac{R_1}{R_2} = \frac{R_3}{R_4} + 1 \rightarrow \frac{R_1}{R_2} = \frac{R_3}{R_4}$$

$$\left[v_0 = \left(\frac{R_2}{R_1} + 1 \right) (v_2 - v_1) \right] \quad \left[A_d = \frac{R_2}{R_1} + 1 \right]$$

b) Este apartado es raro

$$|A_{CL}(w\omega)| = \frac{A_{CL0}}{\sqrt{1 + \left| \frac{w\omega}{w_c} \right|^2}} = \frac{A_{CL0}}{\sqrt{2}}$$

- Para v_2



$$\frac{0 - v_-}{R_1} = \frac{v_- - v_0}{R_2} \Rightarrow v_- = v_0 \left(\frac{R_1}{R_1 + R_2} \right)$$

$$\beta = \frac{R_1}{R_1 + R_2} = \frac{1}{1 + 9} = 0.1$$

$$BW_2 = 0.1 \cdot f_T = 0.1 \cdot 20 \text{ MHz} = 2 \text{ MHz}$$

- Para v_1

$$1^a \left\{ \frac{0 - v_1}{R_4} = \frac{v_1 - v_0}{R_3} \rightarrow v_{01} = v_1 \left(1 + \frac{R_3}{R_4} \right) \rightarrow G_1 = \frac{10}{9} \rightarrow \beta = \frac{9}{20} = 0.45 \right.$$

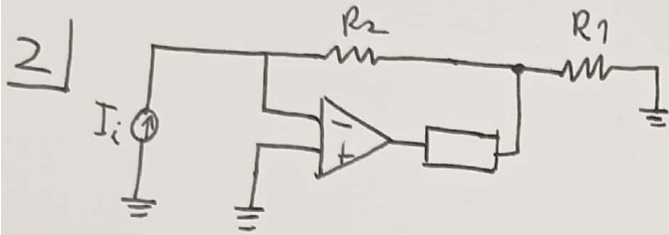
$$2^a \left\{ \frac{v_1 - 0}{R_1} = \frac{0 - v_0}{R_2} \rightarrow v_0 = -\frac{R_2}{R_1} v_1 \rightarrow G_2 = -9 \rightarrow \beta = 0.1 \right.$$

$$|A_{CL0}| = |G_2| |G_1| = 20/1$$

$$\frac{\frac{20}{4}}{\sqrt{1 + \left(\frac{\omega_0}{\beta_1 \omega_{t1}}\right)^2}} \cdot \frac{\omega_0}{\sqrt{1 + \left(\frac{\omega_0}{\beta_2 \omega_{t2}}\right)^2}} = \frac{20}{\sqrt{2}}$$

$$\left(1 + \frac{\omega_0^2}{\beta_1^2 \omega_{t1}^2}\right) \left(1 + \frac{\omega_0^2}{\beta_2^2 \omega_{t2}^2}\right) = 2 \quad (\text{Despejando y todo eso})$$

$$\omega_0^4 + 812 \cdot 10^{11} \omega_0^2 - 811 \cdot 10^{21} = 0 \quad \left[\omega_0 = 98 \text{ kHz} \right]$$



$$I_i = \frac{0 - V}{R_2} \rightarrow V = -I_i R_2$$

$$I_i = \frac{0 - 0}{R_1} + I_0 \rightarrow I_i \left(1 + \frac{R_2}{R_1}\right) = \frac{I_0}{\alpha}$$

$$\left[I_0 = \left(1 + \frac{R_2}{R_1}\right) I_i \right]$$

$$b) I_i = \frac{V - 0}{R_2}$$

$$V_{out} = -A_d V$$

$$I_{in} = \frac{V - 0}{R_1} + I_0 (1)$$

$$V_L = V - V_{out} = V + A_d V$$

$$V_L = I_i R_2 + V \rightarrow V_L - V = I_i R_2 A_d + V A_d \cdot \cancel{A_d(1+A_d)} = V_L - I_i R_2 A_d$$

$$V_L = \frac{V_L - V}{A_d}$$

$$V = \frac{V_L}{1+A_d} - I_i \frac{R_2 A_d}{1+A_d}$$

$$\rightarrow V(1+A_d) = V_L - I_i R_2 A_d$$

$$V = \frac{V_L}{1+A_d} - I_{in} \frac{R_2 A_d}{1+A_d} \quad ; \quad V_i = \frac{V_L}{1+A_d} + I_{in} \frac{R_2}{1+A_d}$$

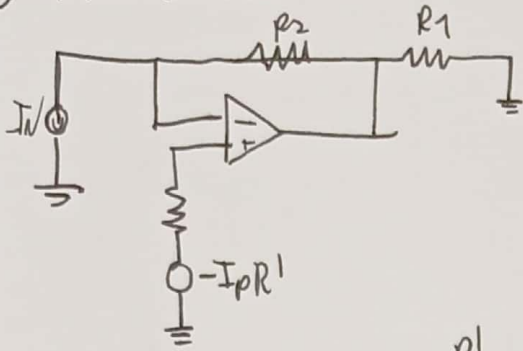
Sust. en 1.

$$I_0 = I_{in} - \frac{V_L}{R_1(1+A_d)} + I_{in} \frac{R_2 A_d}{R_1(1+A_d)}$$

$$I_0 = I_{in} \left(1 + \frac{R_2 A_d}{R_1(1+A_d)}\right) - \frac{V_L}{R_1(1+A_d)} \quad \left\{ \begin{aligned} G_m &= \frac{R_2 A_d}{R_1(1+A_d)} \\ R_L &= R_1(1+A_d) \end{aligned} \right.$$

$$R_L = R_1(1+A_d)$$

c) Introducimos las corrientes de pul. y la resistencia entre



$$v(-) = v(+) = -I_P R1$$

$$I_1 = I_O + I_N \rightarrow I_O = \frac{v - v_A}{R1} - I_N$$

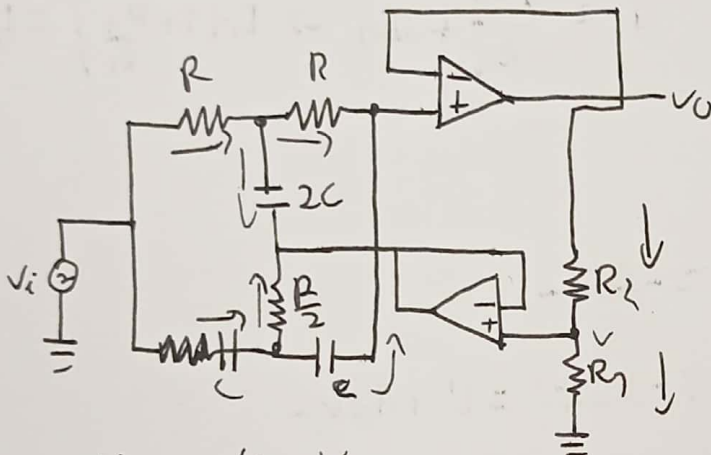
$$I_N = \frac{v_A + I_P R1}{R2} \rightarrow v_A = I_N R2 - I_P R1$$

$$I_O = I_P \frac{R1}{R2} - I_N \left(1 + \frac{R2}{R1}\right)$$

$$\frac{R1}{R2} = 1 + \frac{R2}{R1} \rightarrow R1 = R2 \left(1 + \frac{R2}{R1}\right)$$

$$I_O = \left(1 + \frac{R2}{R1}\right) (I_P - I_N)$$

3



$$\frac{v_i - v_A}{R} = \frac{v_A - v}{1/2Cs} + \frac{v_A - v_O}{R} \rightarrow v_A = \frac{v_i}{2RCs + 2} + v_O \frac{1 + 2CsR}{2(RCs + 1)}$$

$$\frac{v_i - v_B}{1/Cs} = \frac{v_B - v}{R/2} + \frac{v_B - v_O}{1/Cs} \rightarrow v_B = v_i \frac{RCs}{2(1 + RCs)} + v_{out} \frac{RCs + 2}{2(1 + RCs)}$$

$$\frac{v_A - v_O}{R} + \frac{v_B - v_O}{1/Cs} = 0 \quad (3)$$

$$\frac{v_O - v}{R2} = \frac{v - 0}{R1} \rightarrow \frac{v_O}{R2} = v \left(\frac{1}{R2} + \frac{1}{R1} \right) \rightarrow \frac{v_O}{\left(1 + \frac{R2}{R1}\right)} = v \rightarrow v = 2v_O$$

Juntamos todo en 3 y despejamos $\frac{v_{out}}{v_{in}}$

$$G = \frac{v_{out}}{v_{in}} = \frac{s^2 + \frac{1}{R2^2 C^2}}{s^2 + \frac{4(1-2)s}{RC} + \frac{1}{R2^2 C^2}}$$

banda eliminada

Calculamos los parámetros $G(s) = \frac{H_0(s^2 + \omega_n^2)}{s^2 + \frac{\omega_0}{Q}s + \omega_0^2}$

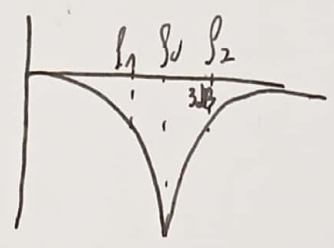
$\omega_0 = \frac{1}{RC} = 377136 \rightarrow f_0 = \frac{\omega_0}{2\pi} = 60 \text{ kHz}$

$H_0 = 1 \rightarrow \frac{\omega_0}{Q} = \frac{4(1-2)}{RC} \rightarrow Q = 29$

Calculamos f_1 y f_2

$f_1 f_2 = f_0^2$
 $BW = \frac{f_0}{Q} = f_2 - f_1$

$f_1^2 + \frac{f_0}{Q} f_1 - f_0^2 = 0$ $\left\{ \begin{array}{l} f_1 = 61'27 \text{ Hz} \\ f_2 = 58'81 \text{ Hz} \end{array} \right.$



4) ADC 3 bits $V_{ref} = 5V$ $V_0 = \{0,125, 0,25, 0,375, 0,5, 0,625, 0,75, 0,875\}$

$V_{LSB} = \frac{V_{ref}}{2^n} = 0,625$

$E_{off} = \frac{V_0(000)}{V_{LSB}} - \frac{1}{2} L_{SN} = \frac{0,125}{0,625} - \frac{1}{2} = -0,125 \text{ B}$

$E_g = \left(\frac{V_0(111)}{V_{LSB}} - \frac{V(001)}{V_{LSB}} \right) - (2^n - 2) = 0,688 \text{ LSB}$

Compensamos $\rightarrow V_{out|comp} = V_{out} - E_{off} - \frac{i E_g}{2^n - 2}$

$V_{comp} = \{0,15, 0,275, 0,4, 0,525, 0,65, 0,775, 0,9\}$

$DNL E_j = \frac{V_{j+1} - V_j - V_{LSB}}{V_{LSB}} = V_{j+1} - V_j - 1$

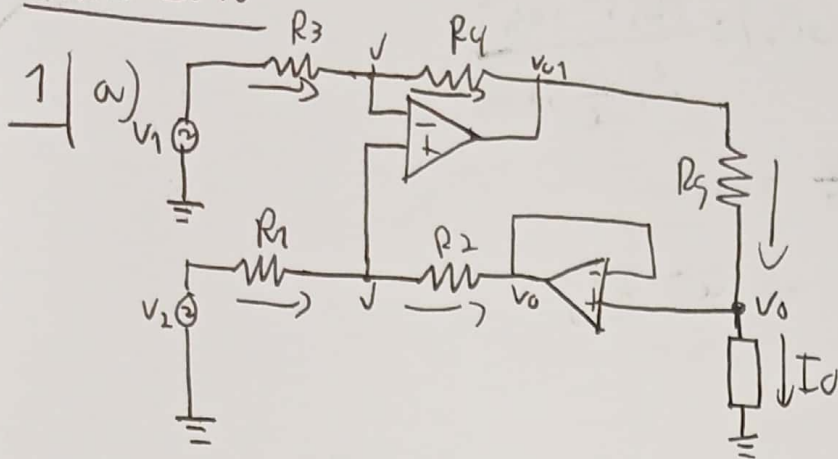
$DNL E = \{0, -0,074, -0,299, 0,175, -0,042, -0,074, 0,262\} \text{ LSB}$

$INLE_j = \sum_{k=0}^j DNL E_k$

$INLE = \{0, -0,074, -0,292, -0,142, -0,180, -0,178, 0,0004\} \text{ LSB}$

Debería ser 0

Enero 2018



$$\frac{v_1 - V}{R_3} = \frac{V - v_{01}}{R_4} \quad (1)$$

$$\frac{v_2 - V}{R_1} = \frac{V - v_0}{R_2} \quad (2)$$

$$\frac{v_{01} - v_0}{R_5} = I_0 \quad (3)$$

$$1) \quad V = v_1 \frac{R_4}{R_3 + R_4} + \frac{R_3}{R_3 + R_4} v_{01}$$

$$2) \quad V = v_0 \frac{R_1}{R_1 + R_2} + v_2 \frac{R_2}{R_1 + R_2}$$

$$v_{01} = v_0 \frac{R_1(R_3 + R_4)}{R_3(R_1 + R_2)} + v_2 \frac{R_2(R_3 + R_4)}{R_3(R_1 + R_2)}$$

$$I_0 = \frac{v_{out}}{R_5} \left(\frac{R_1(R_3 + R_4)}{R_3(R_1 + R_2)} - 1 \right) + v_2 \frac{R_2(R_3 + R_4)}{R_5 R_3 (R_1 + R_2)} - v_1 \frac{R_4}{R_5 R_3}$$

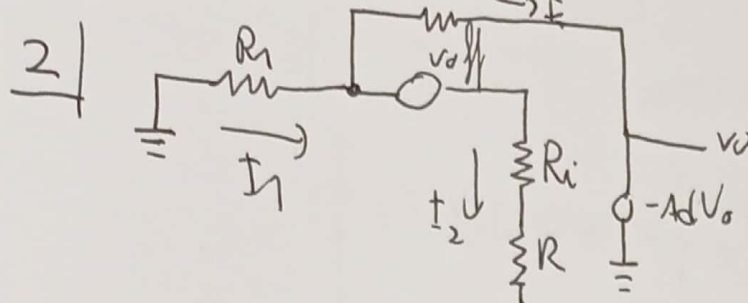
$$I_0 = A_1 v_2 - A_2 v_1 - \frac{v_{out}}{R_0}$$

$$\frac{1}{R_5} \left(1 - \frac{R_1(R_3 + R_4)}{R_3(R_1 + R_2)} \right) = 0 \rightarrow \left[\frac{R_2}{R_1} = \frac{R_4}{R_3} \right]$$

Por lo que

$$I_0 = \frac{R_2}{R_5 R_1} (v_2 - v_1)$$

b) Pasa, meter unentes por y resolver



$$I_1 = I_2 + I_d$$

$$I_2 = \frac{V_d}{R_i} = \frac{V - V_{off}}{R_1 + R_2}$$

$$\frac{0 - V}{R_1} = \frac{V - V_{off}}{R_1 + R_2} + \frac{V - V_{out}}{R_2} \Rightarrow V = V_{off} + V_d \frac{R_1 + R_2}{R_i} = V_{off} - V_{out} \frac{R_1 + R_2}{A_d R_i}$$

$$\hookrightarrow V \left(\frac{1}{R_1} + \frac{1}{R_1 + R_2} + \frac{1}{R_2} \right) = \frac{V_{off}}{R_1 + R_2} + \frac{V_{out}}{R_2}$$

Juntas $V_{out} = \frac{A_d R_i (R_1 + R_2)}{R_1 R_i A_d + (R_1 + R_2)(R_2 + R_1) + R_1 R_2}$

Si $A_d = \infty \rightarrow V_{out} = \frac{R_1 + R_2}{R} V_{off}$

3) Metemos vx al principio

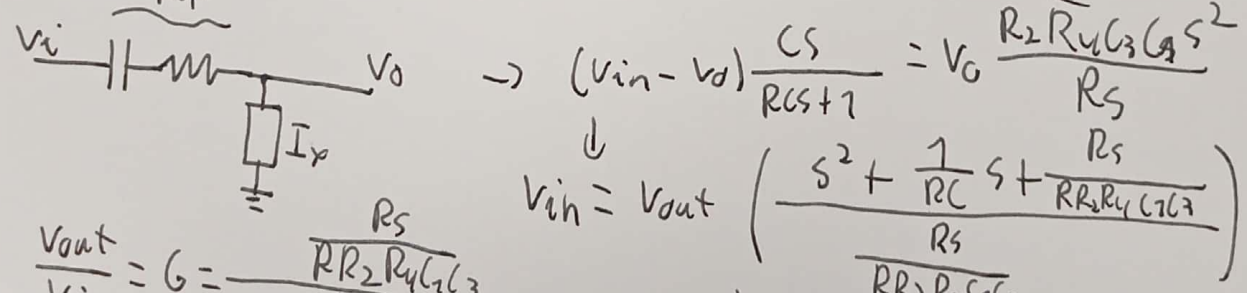
$-I_4 = I_5$

$$\frac{V_1 - V_x}{R_4} = \frac{V_2 - 0}{R_5} \rightarrow V_1 = V_x \left(1 + \frac{R_4}{R_5} \right)$$

$-I_2 = I_3$

$$\frac{V_2 - V_x}{R_2} = (V_0 - V_1) C_3 S \rightarrow V_2 = \left(1 - \frac{R_2 R_4 C_3 S}{R_5} \right) V_x$$

$-I_x = (V_x - V_2) C_1 S \rightarrow I_x = V_x \frac{R_2 R_4 C_3 C_1 S^2}{R_5} \rightarrow \left[Z_{eq} = \frac{V_x}{I_x} = \frac{R_5}{R_2 R_4 C_3 C_1 S^2} \right]$



$$(V_{in} - V_0) \frac{C_1 S}{R_4 S + 1} = V_0 \frac{R_2 R_4 C_3 C_1 S^2}{R_5}$$

$$V_{in} = V_{out} \left(\frac{S^2 + \frac{1}{R_4 C_1} S + \frac{R_5}{R_2 R_4 C_1 C_3}}{R_5} \right)$$

$$\frac{V_{out}}{V_{in}} = G = \frac{R_5}{S^2 + \frac{1}{R_4 C_1} S + \frac{R_5}{R_2 R_4 C_1 C_3}}$$

pasa baja

$$\omega_0 = \sqrt{\frac{R_5}{R_2 R_4 C_1 C_3}} = 5039 \rightarrow f_{oi} = \frac{\omega}{2\pi} = 802 \text{ Hz} ; H_0 = 1$$

$$\frac{\omega}{Q} = \frac{1}{R_4 C_1} \rightarrow Q = 3.97 \approx 4$$

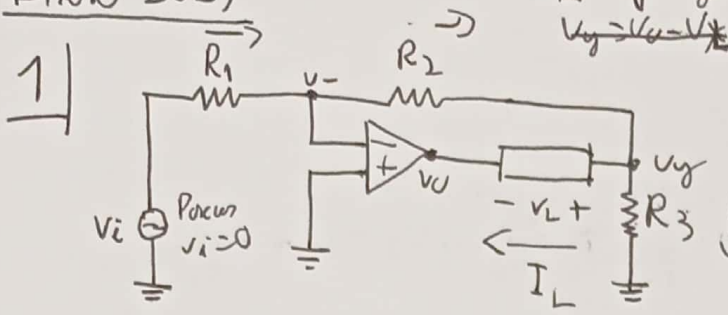
$$b) \omega_{max} = \omega_0 \sqrt{1 - \frac{1}{2Q^2}} = 4958'43 \text{ Hz}$$

$$20 \log_{10} |G(j\omega_{max})| = 20 \log_{10} \left| \frac{K_0 K_0}{\sqrt{1 - \frac{1}{4Q^2}}} \right| = 12'04 \text{ dB}$$

$$20 \log_{10} |G(j\omega)| = 20 \log_{10} |K_0 K_0| = 11'97 \text{ dB}$$



4) El mismo que el anterior



$v_L = v_o - v_i$
 $v_o = (v_+ - v_-) A_d = -A_d v_-$
 $v_- = -\frac{v_o}{A_d}$

$1) \frac{-v_-}{R_1} = \frac{v_- - v_o}{R_2}$
 $2) \frac{v_- - v_o}{R_2} = I_L + \frac{v_o - v}{R_3}$

$v_L = v_o - v_i \rightarrow v_o = v_L + v_i = v_L - A_d v_-$

$1) \frac{-v_-}{R_1} = \frac{v_- - v_o}{R_2} \rightarrow \frac{v_L}{R_2} = v_- \left[\frac{1}{R_1} + \frac{1}{R_2} + \frac{A_d}{R_2} \right]$

$v_L = v_- \left[\frac{R_2}{R_1} + 1 + A_d \right]$

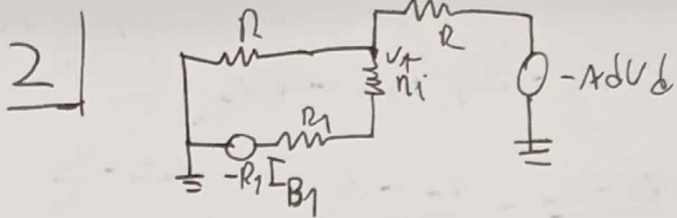
$v_- = v_L \frac{1}{\left[\frac{R_2}{R_1} + 1 + A_d \right]}$

$v_o = v_L - A_d v_- = v_L \left[1 - \frac{A_d}{\left[\frac{R_2}{R_1} + 1 + A_d \right]} \right]$

$I_L = +\frac{v_-}{R_2} - v_o \left[\frac{1}{R_2} - \frac{1}{R_3} \right] = \frac{v_L}{\left[\frac{R_2}{R_1} + 1 + A_d \right] R_2} - v_L \left[1 - \frac{A_d}{\left[\frac{R_2}{R_1} + 1 + A_d \right]} \right] \left[\frac{1}{R_2} - \frac{1}{R_3} \right]$

$I_L = v_L \left[\frac{1}{R_2 \left[\frac{R_2}{R_1} + 1 + A_d \right]} - \left[1 - \frac{A_d}{\left[\frac{R_2}{R_1} + 1 + A_d \right]} \right] \left[\frac{1}{R_2} - \frac{1}{R_3} \right] \right]$

$Z_L = \frac{v_L}{I_L} = -\frac{R_3 \left[R_1(1+A_d) + R_3 \right]}{R_1 + R_2 + R_3} = -507 \text{ k}\Omega$



$$\frac{0 - V_A}{R} = \frac{V_A - V_O}{R} + \frac{V_d}{n_i} \rightarrow \frac{V_O}{R} = \frac{2V_A}{R} + \frac{V_d}{n_i} \rightarrow V_O = 2V_A + \frac{V_d}{n_i} R$$

$$\frac{V_d}{n_i} = \frac{V_A - (-n_i I_{B1})}{n_i + n_i} = \frac{n_i I_{B1} V_A - n_i^2 I_{B1}}{2n_i} \quad \left. \begin{array}{l} n_i \approx h_i \\ -A_d n_i \end{array} \right\}$$

$$V_O = \frac{-2n_i R I_{B1} A_d}{4n_i + 2(R_i + R)} I_{B1}$$

3) ADC $n=4$ $V_{ref} = 3V$ $C = 8pF$ $C_p = 4pF = \frac{C}{2}$ $V_i = 2.1V$

- Ciclo de muestreo
Toda a tierra y a V_i

$$Q = C_{eq} \Delta V = 2C V_i$$

- Ciclo de retención abran suro por lo que C_p afecta.

La carga se conecta

$$Q_1 = Q_p \rightarrow 2C V_i = -(2C + C_p) V_p \rightarrow V_p = -\frac{2C}{2C + C_p} V_i = -1.92V$$

- Ciclo de redistrib. de carga

- Conectar C a V_{ref}

$$(V_{ref} - V_1) C = C_{eq} V_1 \rightarrow V_1 = \frac{C}{2C + C_p} V_{ref} = 1.22V$$

$$V_p + V_1 = -0.72V < 0 \rightarrow b_0 = 1$$

- Conectar C y $\frac{C}{2}$ a V_{ref}

$$(V_{ref} - V_2) (C + \frac{C}{2}) = C_{eq} V_2 \rightarrow V_2 = \frac{C + \frac{C}{2}}{2C + C_p} V_{ref} = 1.8V$$

$$V_p + V_2 = -0.12V \rightarrow b_2 = 1$$

- Conectar C , $\frac{C}{2}$ y $\frac{C}{4}$ a V_{ref}

$$(V_{ref} - V_3) (C + \frac{C}{2} + \frac{C}{4}) = C_{eq} V_3 \rightarrow V_3 = \frac{C + \frac{C}{2} + \frac{C}{4}}{2C + C_p} V_{ref} = 2.25V$$

$$V_p + V_3 = 0.18V > 0 \rightarrow b_3 = 0$$

- Conectar C , $\frac{C}{2}$, $\frac{C}{4}$ y $\frac{C}{8}$ a V_{ref}

$$V_4 = \frac{C + \frac{C}{2} + \frac{C}{4} + \frac{C}{8}}{2C + C_p} V_{ref} = 0.03V > 0 \rightarrow b_4 = 0$$

$$V_{out} = V_{ref} \left(\frac{1}{2} + \frac{1}{4} + \frac{0}{8} + \frac{0}{16} \right) = 2.25V \quad \left. \begin{array}{l} \text{Codigo } 1100 \\ \rightarrow E = \frac{V_O - V_i}{\frac{3}{2^4}} = -0.18LSB \end{array} \right\}$$